# Lecture 2 – Random Testing AAA705: Software Testing and Quality Assurance

Jihyeok Park

PLRG

2024 Spring

# Recall



- Equivalence Partitioning (EP)
- Boundary Value Analysis (BVA)
- Category Partition Method (CPM)
- Combinatorial Testing (CT)
  - Covering Array (CA)
  - Fault Detection Effectiveness
  - Greedy Algorithm IPOG Strategy
  - Greedy vs. Meta-heuristic

#### PLRG

# Contents

#### 1. Random Testing (RT)

Probabilistic Analysis Weaknesses of Random Testing Examples

#### 2. Adaptive Random Testing (ART)

Levenshtein (Edit) Distance Distance Comparison Target Complexity of ART Quasi-Random Strategy for ART

#### 3. Fuzz Testing

Pre-process Input Generation – Mutation-Based Fuzzing Input Generation – Generation-Based Fuzzing Test Oracles (Sanitizers) De-duplication

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- We need to **sample** the test input from the vast and possibly infinite **input space**.
- What happens if we just sample the input **randomly**?
  - Since developers has their own mental model of the software, they often have a **biased** view of the input space.
  - Random testing can help to ignore this bias.



• SUT: Software Under Test



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- S: Set of all possible test inputs for SUT



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- S: Set of all possible test inputs for SUT
- F: a subset of S a set of all failing test inputs



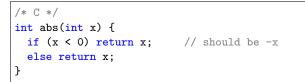
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Failure Rate 
$$t = \frac{|F|}{|S|}$$

(The probability that a randomly sampled test input is fail when we sample uniformly at random from S)

# Random Testing – Example





- Failure Rate  $t \approx 0.5$
- Oracle
  - assertEqual(abs(-5), 5)
  - assertEqual(abs(5), 5)



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  - Xorshift Fast but fail some tests / variants (xorshift+, xoshiro, etc.)
- True-random number generators (TRNGs) expensive
  - Atmospheric noise https://random.org
  - Quantum random number generator (QRNG) https://qrng.anu.edu.au
  - Lava lamps Cloudflare

<sup>2</sup>https://github.com/php/php-src/commit/a0724d

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<sup>&</sup>lt;sup>1</sup>https://bugs.php.net/bug.php?id=75170





The new Galaxy Quantum 4 is equipped with the world's smallest (width 2.5mm x length 2.5mm) **Quantum Random Number Generator (QRNG)** chipset, enabling trusted authentication and encryption of information.

#### Probabilistic Analysis



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# Probabilistic Analysis



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# Probabilistic Analysis



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- Given a failure rate *p*, **how many** test inputs do we need to sample to find the **first failure**?
- Given *n* random test inputs, what is the **probability** of finding **at least one failure**?

• The **geometric distribution** models the first occurrence of a success in a sequence of *n* independent (Bernoulli) trials with the same probability *p*.

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- The most popular example is the coin flipping.
- The **probability mass function (PMF)** of the geometric distribution:

$$Pr(X = k) = (1 - p)^{k-1}p$$

It is the probability that the first success occurs on the *n*-th trial.



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- Given a failure rate *p*, **how many** test inputs do we need to sample to find the **first failure**?
- Mean (If p = 0.01, the average test inputs = 100)

$$\frac{1}{p}$$

• Median (If p = 0.01, the median test inputs  $\approx 69$ )

$$\left\lceil \frac{-1}{\log_2(1-p)} \right\rceil$$

• Variance (If p = 0.01, the variance = 9900)

$$\frac{1-p}{p^2}$$



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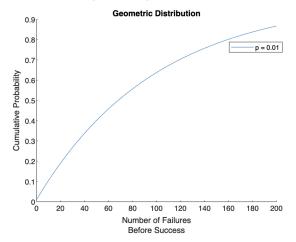
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=  $1 - (1 - p)^{n}$ 

- If we test n = 100 random test inputs, the probability of finding at least one failure is  $1 (1 0.01)^{100} = 63.76\%$ .
- If we test n = 200 random test inputs, the probability of finding at least one failure is  $1 (1 0.01)^{200} = 86.74\%$ .





- Unfortunately, failure rate *p* is **unknown** in practice.
- But, we can **estimate** *p* in various ways:
  - Previous versions of the software
  - Similar software
  - Literature

#### Weaknesses of Random Testing



 Random testing provides no guidance; it is the needle in a haystack problem – the probability of finding a failure is low.

```
/* C */
void foo(int x) {
    if (x == 0) {
        /* faulty code here */
    }
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# Python
def foo(x):
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- We need **biased** random testing with predefined probability:
  - Special values (-0, null, π, ...)
  - Extracted values from code (e.g., constants, literals)
  - Previously successful values



• **Apple** (1983) - "Monkey" for random events (e.g., mouse clicks, key presses, etc.) to test the robustness of the MacWrite and MacPaint applications.



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- **Netflix** (2011) "**Chaos Monkey**" that randomly terminates AWS instances to test the fault tolerance of the Netflix infrastructure.

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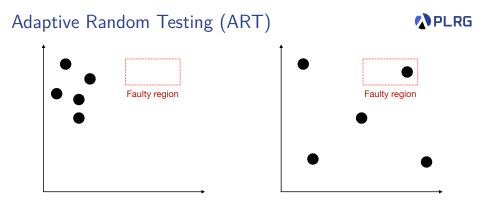


• **Insight** – failing test inputs often **cluster** in the input space.

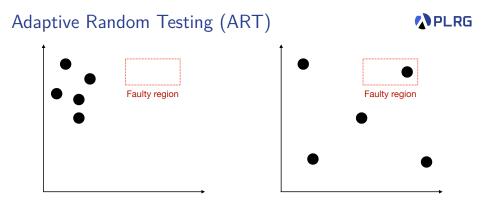
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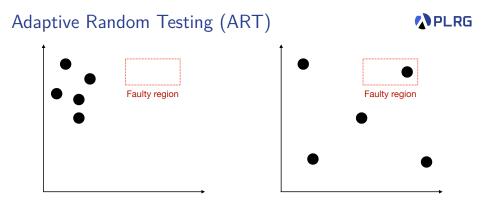
• Without knowing the faulty regions, what is the **best way** to sample the test inputs?



• A more **diverse** set of test inputs is more likely to find a failure.

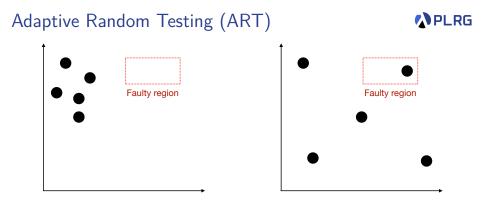


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• Then, how to measure the distance between complex data types?



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- For example, the distance between "kitten" and "sitting" is 3:

$$\text{``kitten''} \xrightarrow[k \to s]{substitute} \text{``sitten''} \xrightarrow[e \to i]{substitute} \text{``sittin''} \xrightarrow[i]{insert} \text{``sitting''}$$



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• and the distance between "uninformed" and "uniform" is 3:

"uninformed" 
$$\xrightarrow[n]{\text{delete}}$$
 "uniformed"  $\xrightarrow[e]{\text{delete}}$  "uniformd"  $\xrightarrow[d]{\text{delete}}$  "uniform"

• The formal definition of the Levenshtein distance is as follows:

$$lev(a, b) = \begin{cases} |a| & \text{if } |b| = 0\\ |b| & \text{if } |a| = 0\\ lev(tail(a), tail(b)) & \text{if } head(a) = head(b)\\ 1 + \min \begin{cases} lev(tail(a), b) & (\text{insert})\\ lev(a, tail(b)) & (\text{delete}) & \text{otherwise}\\ lev(tail(a), tail(b)) & (\text{substitute}) \end{cases}$$



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- It is usually extended into a parameterized version with a set of allowed **edit operations** (e.g., transposition) with different **costs**.
- Wagner-Fischer algorithm (1967) O(mn) time complexity
- Indyk and Bačkurs (2015) proved that the problem of finding the edit distance **cannot be solved in less than quadratic time**. (We cannot do better than the Wagner-Fischer algorithm.)

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$$diversity(T) = \sum_{(t_1,t_2)\in T imes T} d(t_1,t_2)$$



• The **diversity** of a test suite is defined as the **sum of distances** between all pairs of test inputs.

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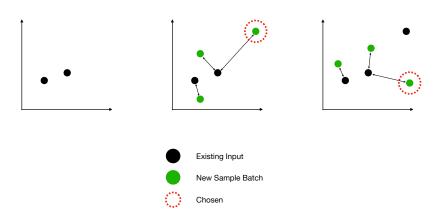
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- Choose the test input that has the **maximum** distance from the existing test inputs.
- Add the **chosen new test input** to the set of existing test inputs.
- Iterate the process until the **stopping criterion** is met.





• It samples *Z* = 3 new test inputs and **chooses** the one with the **maximum distance** from the existing test inputs.

#### Distance Comparison Target



• For each **new test case** *t*, we need to choose the **target for comparison** in the existing test suite *T*.<sup>3</sup>

<sup>3</sup>[CSUR'19] R. Huang et al. "A survey on adaptive random testing."

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Lecture 2 - Random Testing

#### Distance Comparison Target



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Centroid-Distance

$$\underline{\textit{fitness}}(t, T) = d(t, 1/|T| \sum t')$$

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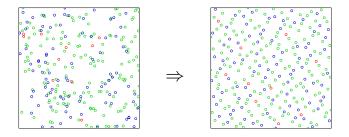


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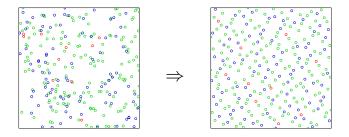
- **O**( $k^2Z$ ) time complexity this could be expensive.
- It may be difficult to choose the meaningful **distance metric** for complex data types.





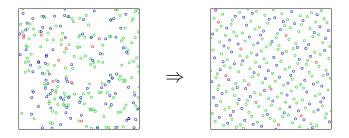
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- What if we can randomly sample the test inputs having **diversity** (i.e., **low discrepancy**)?
- Quasi-random sequences could be a good choice.
- Let's learn **Halton sequence**, one of the representative quasi-random sequences.

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- For example, generate the sequence of numbers in the range [0,1] by recursively splitting the range into 2 or 3 subintervals.

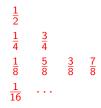
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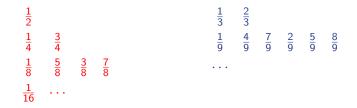
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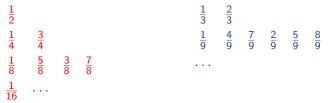
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• Generate a sequence of pairs of numbers (*x*, *y*) by combining above sequences.

$$(\frac{1}{2},\frac{1}{3}),(\frac{1}{4},\frac{2}{3}),(\frac{3}{4},\frac{1}{9}),(\frac{1}{8},\frac{4}{9}),(\frac{5}{8},\frac{7}{9}),(\frac{3}{8},\frac{2}{9}),(\frac{7}{8},\frac{5}{9}),(\frac{1}{16},\frac{8}{9}),\cdots$$



We can utilize other quasi-random sequences for ART:<sup>4</sup>

• Halton Sequence

$$\phi_b(i) = \sum_{j=0}^{\omega} i_j b^{-j-1}$$

Sobol Sequence

$$\mathsf{Sobol}(i) = \mathsf{XOR}_{j=1,2,\cdots,\omega}(i_j\delta_j)$$

where

$$\delta_j = XOR_{k=1,2,\cdots,r} \left(\frac{\beta_k \delta_{j-k}}{2^j}\right) \oplus \frac{\delta_{j-k}}{2^{j+r}}$$

• Niederreiter Sequence

<sup>4</sup>[CSUR'19] R. Huang et al. "A survey on adaptive random testing."

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# Adaptive Random Testing (ART) – Summary

#### • Application Domains

- Numeric Programs
- Object-Oriented Programs
- Configurable Systems
- Web Services and Applications
- Embedded Systems
- Simulations and Models

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# Adaptive Random Testing (ART) – Summary

#### • Application Domains

- Numeric Programs
- Object-Oriented Programs
- Configurable Systems
- Web Services and Applications
- Embedded Systems
- Simulations and Models
- Faulty regions may not apply to all types of faults.
- **ART** is still mostly an academic idea, with debates going on:
  - **[ISSTA'11]** A. Arcuri et al. "Adaptive random testing: an illusion of effectiveness?"
  - [CSUR'19] R. Huang et al. "A survey on adaptive random testing."

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## Contents

#### 1. Random Testing (RT)

Probabilistic Analysis Weaknesses of Random Testing Examples

### 2. Adaptive Random Testing (ART)

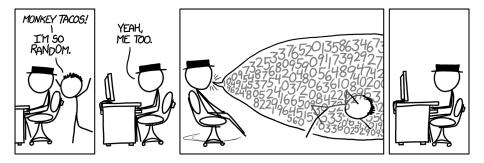
Levenshtein (Edit) Distance Distance Comparison Target Complexity of ART Quasi-Random Strategy for ART

#### 3. Fuzz Testing

Pre-process Input Generation – Mutation-Based Fuzzing Input Generation – Generation-Based Fuzzing Test Oracles (Sanitizers) De-duplication







https://xkcd.com/1210/



• **[CACM'90]** B. P. Miller et al. "An empirical study of the reliability of UNIX utilities."<sup>5</sup>

"On a dark and stormy night one of the authors was logged on to his workstation on a dial-up line from home and the rain had affected the phone lines; there were frequent spurious characters on the line. The author had to race to see if he could type a sensible sequence of characters before the noise scrambled the command. This line noise was not surprising; but we were surprised that these spurious characters were causing programs to crash."

<sup>5</sup>https://alastairreid.github.io/RelatedWork/papers/miller:cacm:1990/





• Fuzz testing is a random testing technique to find exceptional outcomes (e.g., crashes, exceptions, freezes, etc.) of a software system.

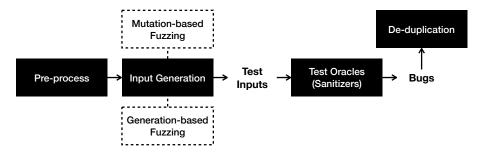




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- 1990 study found crashes in: adb, as, bc, cb, col, diction, emacs, eqn, ftp, indent, lex, look, m4, make, nroff, plot, prolog, ptx, refer!, spell, style, tsort, uniq, vgrind, vi

## Fuzz Testing - Overview

### PLRG



- Pre-process prepare the SUT for fuzz testing
- Input Generation generate test inputs
  - Mutation-Based Fuzzing modify existing test inputs
  - Generation-Based Fuzzing generate new test inputs
- Test Oracles (Sanitizers) detect exceptional outcomes
- De-duplication remove duplicate test inputs



 Instrumentation – source-level or binary-level modification of the SUT to collect information about the execution in compile time (static) or runtime (dynamic).



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  - Libraries a driver program that calls functions in the library
  - Kernels may fuzz user-land applications to test kernels
  - **IoT devices** a driver communicate with the corresponding smartphone application.

## Input Generation – Mutation-Based Fuzzing

Initial → Seed → Seed Selection → Seeds Pool → Seed Selection → Seeds Interesting Seeds Seed Mutation ↓ Seed Trimming New Seeds

• In the mutation-based fuzzing, a **seed** is a test input that is used to generate new test inputs.

## Input Generation – Mutation-Based Fuzzing

Initial Seeds → Seed → Seed Selection → Seeds Interesting Seeds Seed Mutation Seed Trimming ← New Seeds

- In the mutation-based fuzzing, a **seed** is a test input that is used to generate new test inputs.
- Mutation-Based Fuzzing first initializes seed pool with the initial seeds, and then mutates them to generate new test inputs and updates the seed pool when a new test input is interesting.

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## Input Generation – Mutation-Based Fuzzing

• Initial Seeds – from the existing test suite, manually crafted, inferred from the SUT or specification.

<sup>6</sup>**[ICSE'21]** J. Park et al. "JEST: N+1-version Differential Testing of Both JavaScript Engines and Specification."

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- Initial Seeds from the existing test suite, manually crafted, inferred from the SUT or specification.
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  - **Bit-Flip** flip a random bit in the seed
  - Arithmetic Mutation add, subtract, multiply, divide, etc.
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  - Semantic-aware Mutation<sup>6</sup> mutate seeds using spec. of SUT

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- Seed Trimming filter out the uninteresting test inputs (e.g., no coverage increase).

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**Generation-Based Fuzzing** generates new test inputs from a **model** that represents the **input space** of the SUT.

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- Encoder Model generates test inputs for decoder programs (e.g., image decoders, audio decoders, etc.) using the corresponding encoder programs.



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- They are usually **instrumented** into the SUT to collect information about the execution in compile time (**static**) or runtime (**dynamic**) with **runtime overhead**.



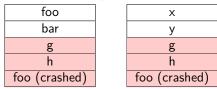
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- **Coverage-based De-duplication** compare the **coverage** of the test inputs (e.g., node, branch, grammar, semantics, etc.)
- Semantic-aware De-duplication compare the semantics of the test inputs (e.g., backward data-flow analysis for blaming)



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• AFL++ (American Fuzzy Lop Plus Plus)

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• **ClusterFuzz** developed by Google

https://google.github.io/clusterfuzz

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#### Next Lecture



• Coverage Criteria

Jihyeok Park jihyeok\_park@korea.ac.kr https://plrg.korea.ac.kr