

# Lecture 6 – Dynamic Symbolic Execution (DSE)

AAA705: Software Testing and Quality Assurance

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2024 Spring

- **Search Based Software Engineering (SBSE)**

- Fitness Landscape
- Local Search
  - Hill Climbing
  - Simulated Annealing
  - Tabu Search
- Genetic Algorithms
  - Selection Strategies
  - Crossover Operators
  - Mutation Operators
- Bio-inspired Algorithms
  - Particle Swarm Optimization (PSO)
  - Ant Colony Optimization (ACO)

- **Search Based Software Testing (SBST)**

- Alternating Variable Method (AVM)

Sometimes called **structural testing** because it uses the **internal structure** of the program to derive test cases.

- **Coverage Criteria**

- The adequacy of a test suite is measured in terms of the **coverage** of the program's internal structure.

- **Search Based Software Testing (SBST)**

- A technique that uses **meta-heuristic search** algorithms to maximize/minimize a certain **fitness function**.

- **Dynamic Symbolic Execution (DSE)**

- A technique that systematically explores the input space using **symbolic execution** with **dynamic analysis**.

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- A technique that systematically explores the input space using **symbolic execution** with **dynamic analysis**.

Let's focus on the **Dynamic Symbolic Execution (DSE)** technique.

## 1. Symbolic Execution

- Basic Idea

- Satisfiability Modulo Theories (SMT)

- Limitations of Symbolic Execution

## 2. Dynamic Symbolic Execution (DSE)

- Search Heuristics

- Example – Hash Function

- Example – Loops

- Example – Data Structures

- Realistic Implementation

- Other Hybrid Analysis Techniques

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- The bug can only be triggered when the input is  $x = 93589$ .
- It means that the probability of triggering the bug is as follows when the integer input is randomly generated:

$$\frac{1}{2^{32}} \approx 0.00000000023283\%$$

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- **1976** – A system to generate test data and symbolically execute programs (Lori Clarke).
- **1977** – Symbolic execution and program testing (James King).
- **2005 to present** – Practical symbolic execution
  - Using advanced constraint solvers (SMT solvers)
  - Heuristics to control exponential path explosion
  - Heap modeling and reasoning about complex data structures
  - Environment modeling
  - Dealing with solver limitations

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- 4 All paths in the program form its **execution tree**, in which some paths are **feasible** and some are **infeasible**.

# Symbolic Execution – Basic Idea

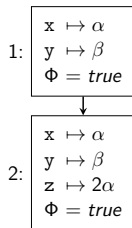
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void f(int x, int y) {  
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```

1:

$x \mapsto \alpha$
$y \mapsto \beta$
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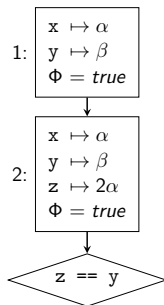
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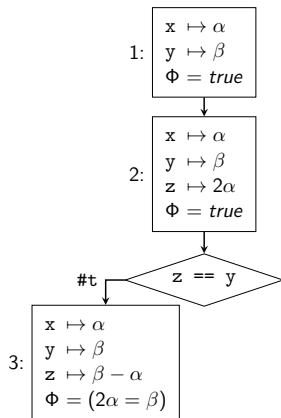
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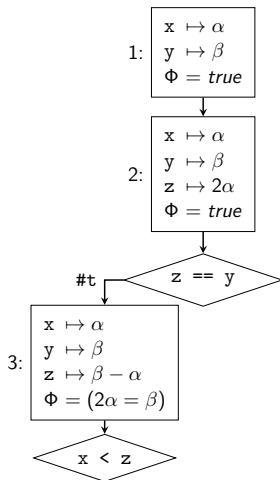
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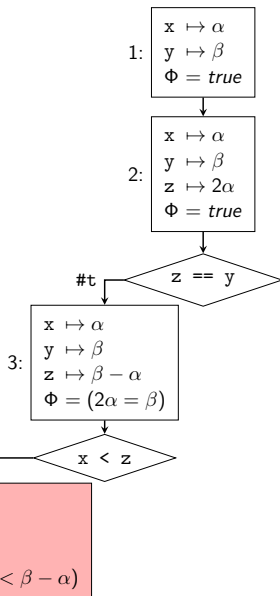
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4:

```
x ↦ α  
y ↦ β  
z ↦ β - α  
Φ = (2α = β) ∧ (α < β - α)
```

**INVALID**

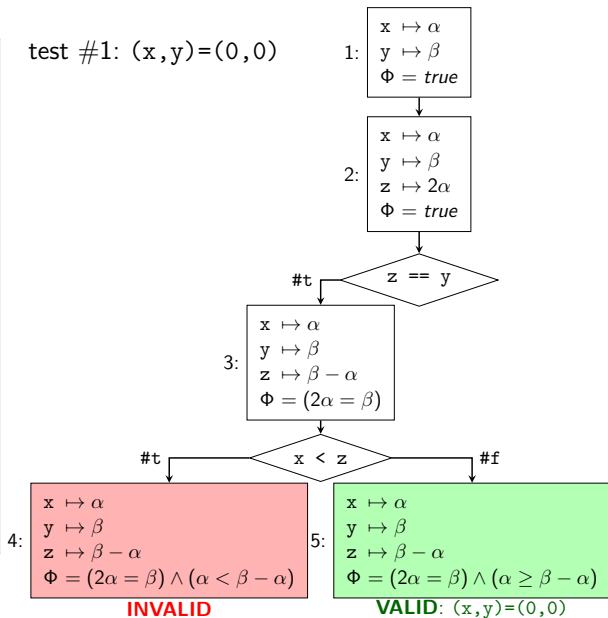




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test #1:  $(x,y)=(0,0)$

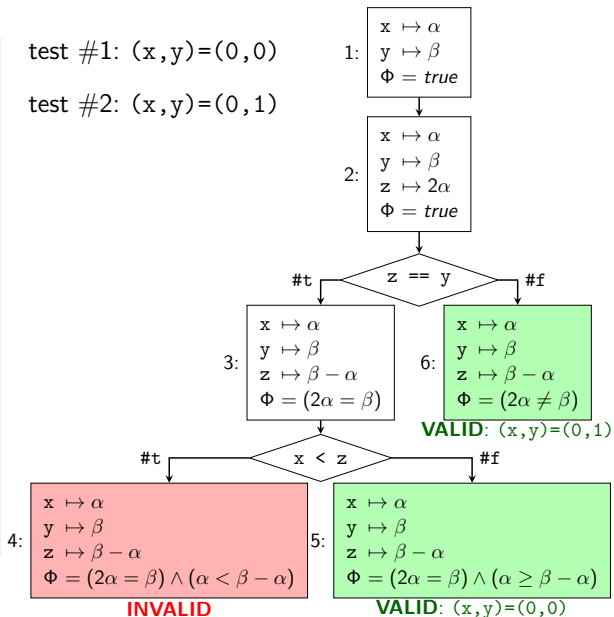


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- Most symbolic execution tools use **Satisfiability Modulo Theories (SMT)** solvers (e.g., Z3, CVC4) to check it.
- An SMT solver takes a **first-order logic formula** and returns whether it is **satisfiable** or not using various background theories, such as arithmetic, arrays, bit-vectors, algebraic data types, etc.

- Check the satisfiability of the following formula using an SMT solver.

$$b + 2 = c \wedge f(\text{read}(\text{write}(a, b, 3), c - 2)) \neq f(c - b + 1)$$

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- **Applying array theory axiom** –  $\forall a, i, v. \text{read}(\text{write}(a, i, v), i) = v.$

$$b + 2 = c \wedge f(3) \neq f(3) \quad (\text{UNSAT})$$

**Z3**<sup>1</sup> is one of the most popular SMT solvers developed by Microsoft Research and used in many symbolic execution tools.

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For example, the following Z3 script returns `unsat`.

```
(declare-const a (Array Int Int))
(declare-const b Int)
(declare-const c Int)
(declare-fun f (Int) Int)
(assert (= (+ b 2) c))
(assert (not (= (f (select (store a b 3) (- c 2))) (f (+ (- c b) 1)))))
(check-sat) ; => unsat
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Or, the following script returns a satisfying assignment  $x = 0$  and  $y = 0$ .

```
(declare-const x Int)
(declare-const y Int)
(assert (and (= (* 2 x) y) (>= x (- y x))))
(check-sat) ; => sat
(get-model) ; => (x, y) = (0, 0)
```

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We cannot solve path condition  $\Phi$  containing the hash function using SMT solver.

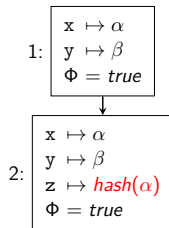
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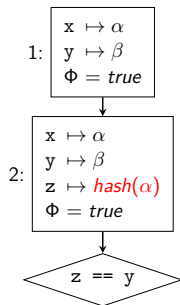
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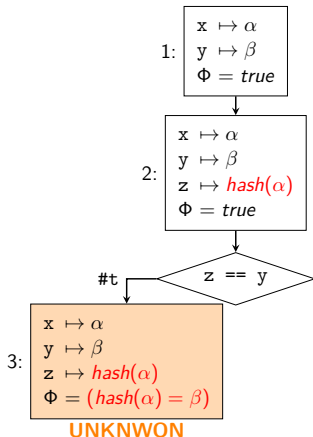
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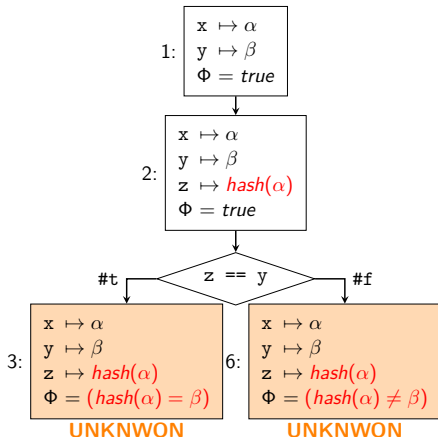




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Satisfiability Modulo Theories (SMT)

Limitations of Symbolic Execution

## 2. Dynamic Symbolic Execution (DSE)

Search Heuristics

Example – Hash Function

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Realistic Implementation

Other Hybrid Analysis Techniques

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- It stores both the **concrete** values and the **symbolic** values during the execution of the program, and solves the path condition to **guide execution** at branch points.
- The concrete values are used to **simplify** the path condition.

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test #1: (x,y)=(3,7)

1:

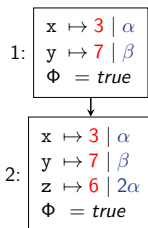
$x \mapsto 3$	$\mid$	$\alpha$
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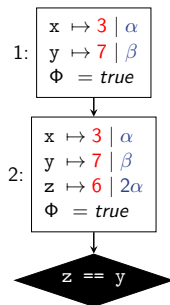


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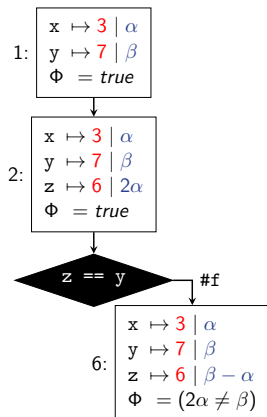


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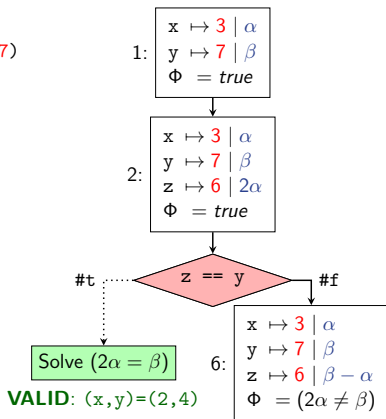
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test #1: (x,y)=(3,7)

test #2: (x,y)=(2,4)

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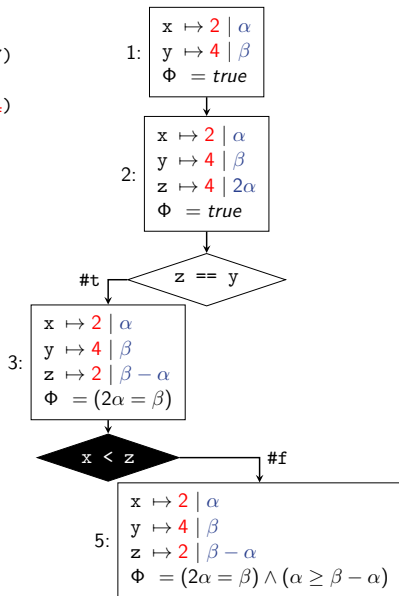
# Dynamic Symbolic Execution (DSE) – Example

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test #1: (x,y)=(3,7)

test #2: (x,y)=(2,4)

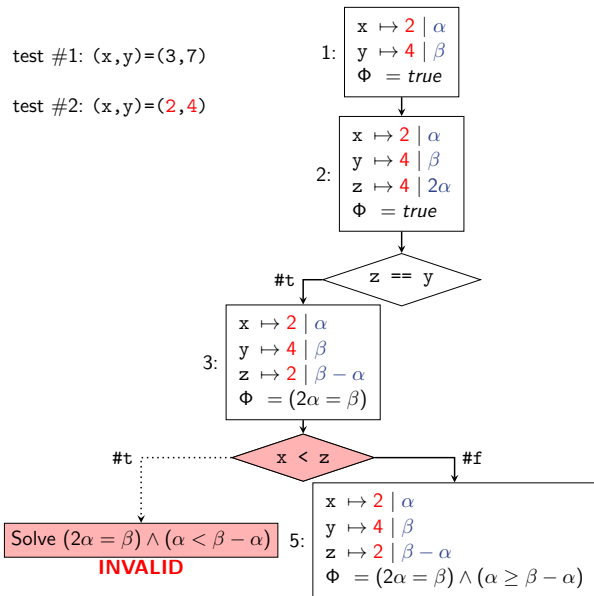


```

void f(int x, int y) {
  /* 1 */
  int z = 2 * x;
  /* 2 */
  if (z == y) {
    z = y - x;
    /* 3 */
    if (x < z) {
      /* 4 */
      ERROR;
    } else {
      /* 5 */
    }
  } else {
    /* 6 */
  }
}
    
```

test #1: (x,y)=(3,7)

test #2: (x,y)=(2,4)



---

## Algorithm 1. Concolic Testing

---

**Input :** Program  $P$ , budget  $N$ , initial input  $v_0$

**Output :** The number of branches covered

```
1:  $T \leftarrow \langle \rangle$ 
2:  $v \leftarrow v_0$ 
3: for  $m = 1$  to  $N$  do
4:    $\Phi_m \leftarrow \text{RunProgram}(P, v)$ 
5:    $T \leftarrow T \cdot \Phi_m$ 
6:   repeat
7:      $(\Phi, \phi_i) \leftarrow \text{Choose}(T)$        $(\Phi = \phi_1 \wedge \dots \wedge \phi_n)$ 
8:     until  $\text{SAT}(\bigwedge_{j < i} \phi_j \wedge \neg \phi_i)$ 
9:      $v \leftarrow \text{model}(\bigwedge_{j < i} \phi_j \wedge \neg \phi_i)$ 
10: return  $|\text{Branches}(T)|$ 
```

---

# Dynamic Symbolic Execution (DSE)

In each iteration, DSE **chooses** a path to explore based on the path condition  $\Phi$  using a specific **search heuristic**.



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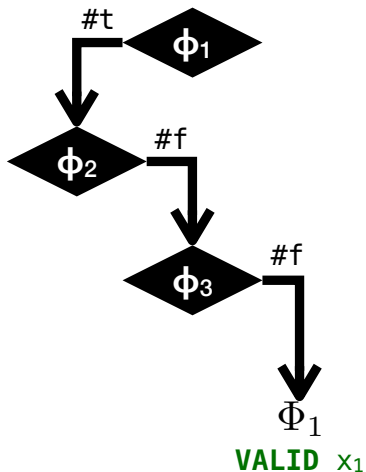
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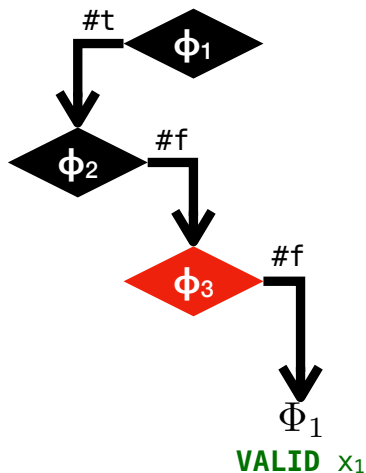
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- etc.

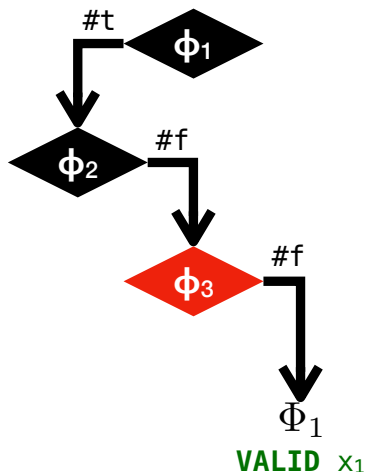
This is the **control-flow directed search (CFDS)** heuristic.



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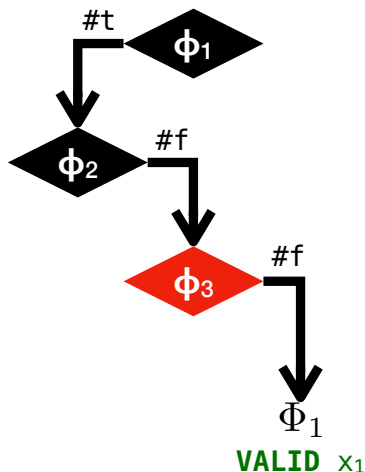
This is the **control-flow directed search (CFDS)** heuristic.



$$\text{Solve } \phi_1 \wedge \neg\phi_2 \wedge \phi_3$$



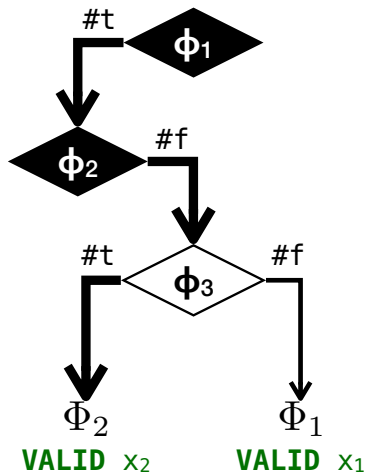
This is the **control-flow directed search (CFDS)** heuristic.



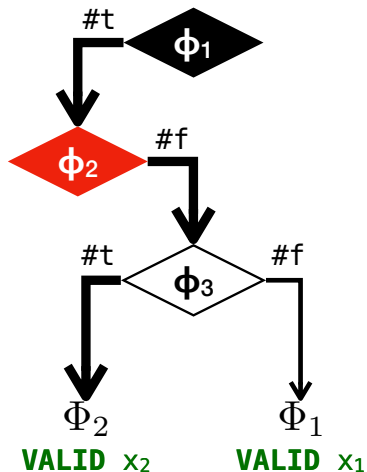
Solve  $\phi_1 \wedge \neg\phi_2 \wedge \phi_3$

**VALID**  $x_2$

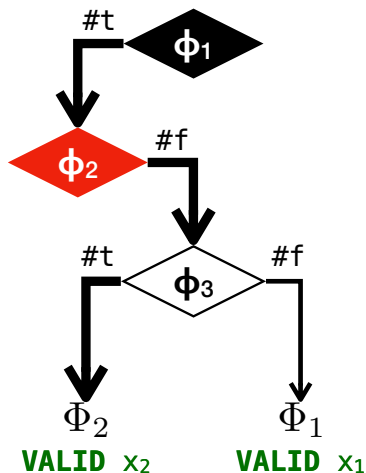
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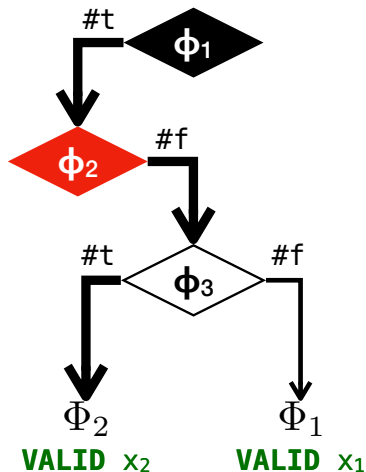


This is the **control-flow directed search (CFDS)** heuristic.



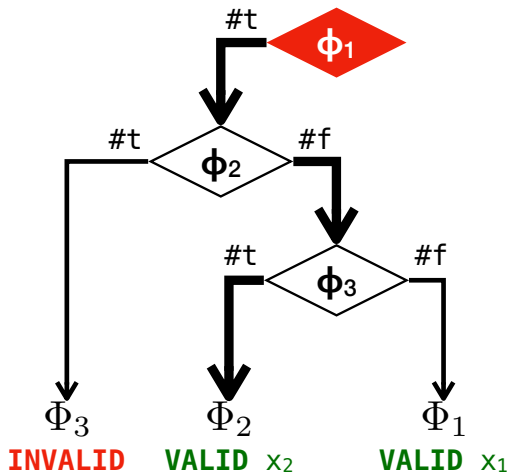
Solve  $\phi_1 \wedge \phi_2$

This is the **control-flow directed search (CFDS)** heuristic.



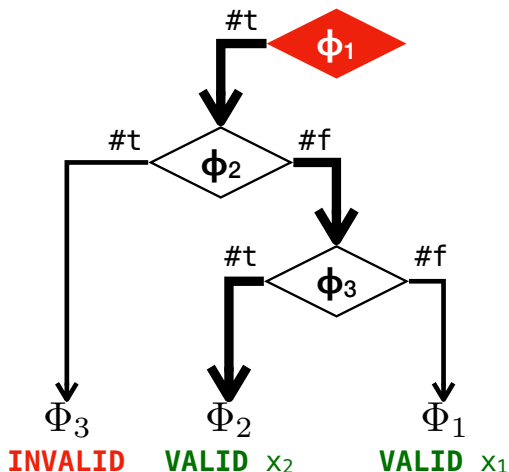
Solve  $\phi_1 \wedge \phi_2$   
**INVALID**

This is the **control-flow directed search (CFDS)** heuristic.

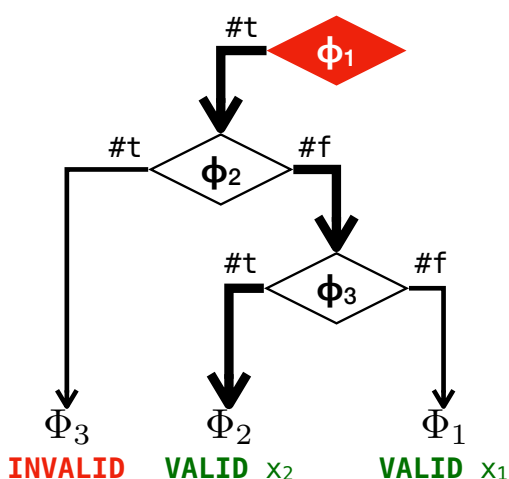


This is the **control-flow directed search (CFDS)** heuristic.

Solve  $\neg\phi_1$



This is the **control-flow directed search (CFDS)** heuristic.

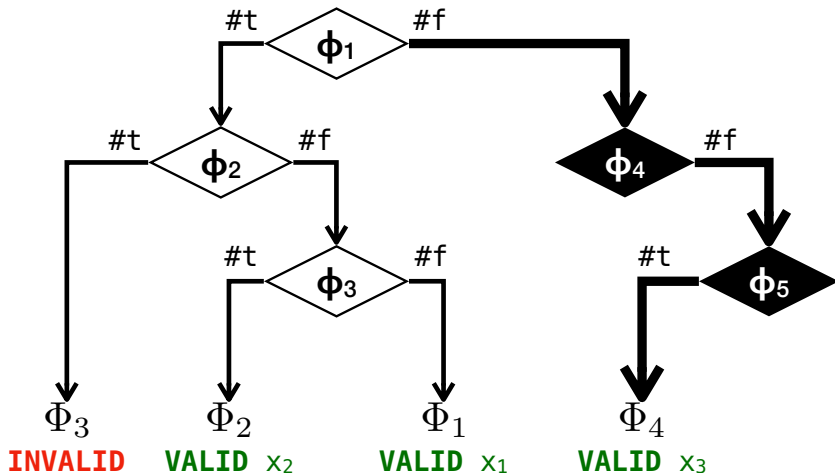


Solve  $\neg\phi_1$

**VALID**  $x_3$



This is the **control-flow directed search (CFDS)** heuristic.



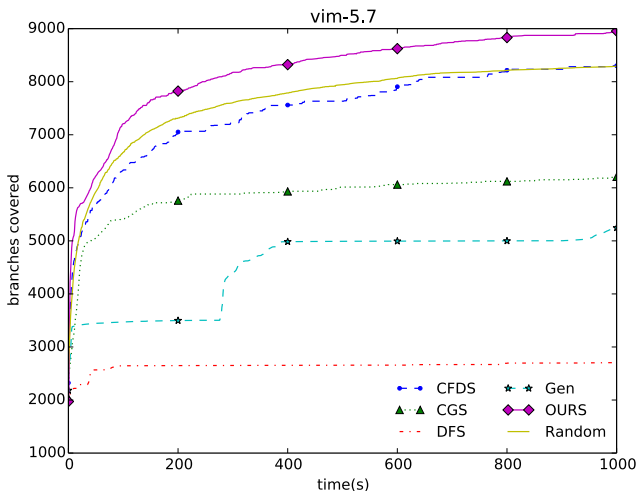
**[ICSE'18]** S. Cha et al., “Automatically Generating Search Heuristics for Concolic Testing”

$$\text{Choose}_\theta(\langle \Phi_1, \dots, \Phi_m \rangle) = (\Phi_m, \underset{\phi_j \in \Phi_m}{\operatorname{argmax}} \operatorname{score}_\theta(\phi_j))$$

Followings are 12 static and 28 dynamic branch features used for learning.

#	Description
1	branch in the main function
2	true branch of a loop
3	false branch of a loop
4	nested branch
5	branch containing external function calls
6	branch containing integer expressions
7	branch containing constant strings
8	branch containing pointer expressions
9	branch containing local variables
10	branch inside a loop body
11	true branch of a case statement
12	false branch of a case statement
13	first 10% branches of a path
14	last 10% branches of a path
15	branch appearing most frequently in a path

**[ICSE'18]** S. Cha et al., "Automatically Generating Search Heuristics for Concolic Testing"



# Example – Hash Function

```
void f(int x, int y) {  
    *  
    int z = hash(x);  
  
    if (z == y) {  
        z = y - x;  
  
        if (x < z) {  
  
            ERROR;  
        } else {  
  
        }  
    } else {  
  
    }  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	7	$\beta$
z		
$\Phi$	true	

```

void f(int x, int y) {

    int z = hash(x);
    *
    if (z == y) {
        z = y - x;

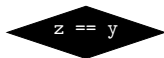
        if (x < z) {

            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	7	$\beta$
z	182039482	$hash(\alpha)$
$\Phi$	true	



```

void f(int x, int y) {

    int z = hash(x);

    if (z == y) {
        z = y - x;

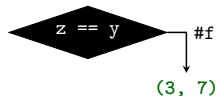
        if (x < z) {

            ERROR;
        } else {

            *
        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	7	$\beta$
z	182039482	$hash(\alpha)$
$\Phi$	$(hash(\alpha) \neq \beta)$	



```

void f(int x, int y) {

    int z = hash(x);

    if (z == y) {
        z = y - x;

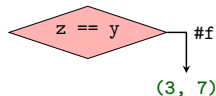
        if (x < z) {

            ERROR;
        } else {

            *
        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	3	$\alpha$
$y$	7	$\beta$
$z$	182039482	$hash(\alpha)$
$\Phi$	$(hash(\alpha) \neq \beta)$	



We can utilize the current concrete values.

$(hash(\alpha) = \beta)$  is **SAT**  
 when  $(x, y) = (3, 182039482)$ .

```

void f(int x, int y) {
    *
    int z = hash(x);

    if (z == y) {
        z = y - x;

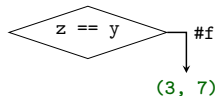
        if (x < z) {

            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	182039482	$\beta$
z		
$\Phi$	true	





```

void f(int x, int y) {

    int z = hash(x);
    *
    if (z == y) {
        z = y - x;

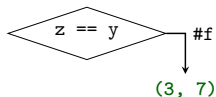
        if (x < z) {

            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	182039482	$\beta$
z	182039482	$hash(\alpha)$
$\Phi$	true	



```

void f(int x, int y) {

    int z = hash(x);

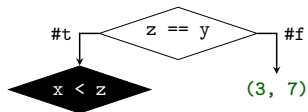
    if (z == y) {
        z = y - x;
        *
        if (x < z) {

            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	182039482	$\beta$
z	182039479	$\beta - \alpha$
$\Phi$	$(hash(\alpha) = \beta)$	



```

void f(int x, int y) {

    int z = hash(x);

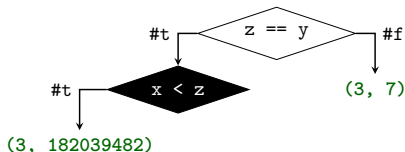
    if (z == y) {
        z = y - x;

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            *
            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
x	3	$\alpha$
y	182039482	$\beta$
z	182039479	$\beta - \alpha$
$\Phi$	$(hash(\alpha) = \beta) \wedge (\alpha < \beta - \alpha)$	



We found an error!

```

void f(int x, int y) {

    int z = hash(x);

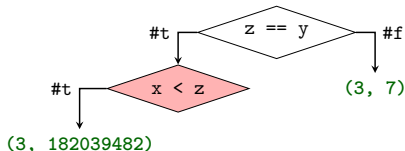
    if (z == y) {
        z = y - x;

        if (x < z) {
            *
            ERROR;
        } else {

        }
    } else {

    }
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	3	$\alpha$
$y$	182039482	$\beta$
$z$	182039479	$\beta - \alpha$
$\Phi$	$(hash(\alpha) = \beta) \wedge (\alpha < \beta - \alpha)$	



Unfortunately,  
 $(hash(\alpha) = \beta) \wedge (\alpha \geq \beta - \alpha)$  is  
**UNKNOWN.**

# Example – Loops

```
void f(int x) {  
    *  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
        if (arr[i] == x) break;  
        i++;  
    }  
  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$		
$i$		
$\Phi$	<i>true</i>	

```
void f(int x) {  
  
    int arr[] = {3, 7, 2};  
    int i = 0;  
    *  
    while (i < 3) {  
  
        if (arr[i] == x) break;  
        i++;  
  
    }  
  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	0	
$\Phi$	<i>true</i>	

# Example – Loops

```
void f(int x) {  
  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
        *  
        if (arr[i] == x) break;  
        i++;  
    }  
  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	0	
$\Phi$	<i>true</i>	

```

void f(int x) {

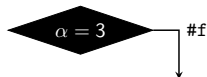
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;
        *
    }

    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	1	
$\Phi$	$(\alpha \neq 3)$	





```

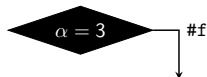
void f(int x) {

    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {
        *
        if (arr[i] == x) break;
        i++;
    }

    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	1	
$\Phi$	$(\alpha \neq 3)$	



```

void f(int x) {

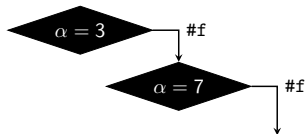
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;
        *
    }

    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	2	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7)$	



```

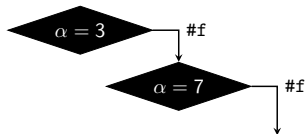
void f(int x) {

    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {
        *
        if (arr[i] == x) break;
        i++;
    }

    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	2	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7)$	



```

void f(int x) {

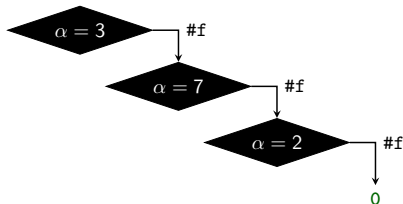
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;
        *
    }

    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	3	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha \neq 2)$	



```

void f(int x) {

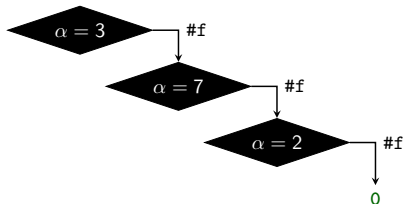
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;

    }
    *
    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	3	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha \neq 2)$	



```

void f(int x) {

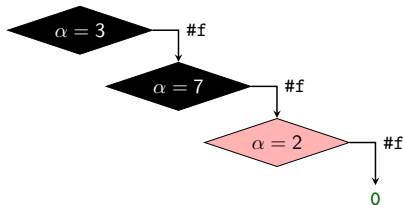
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;

    }
    *
    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$arr$	{3, 7, 2}	
$i$	3	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha \neq 2)$	

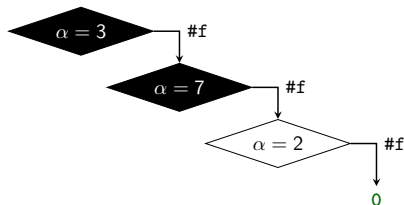


$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha = 2)$  is **SAT**  
when  $x = 2$

# Example – Loops

```
void f(int x) {  
    *  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
        if (arr[i] == x) break;  
        i++;  
    }  
  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	2	$\alpha$
$arr$		
$i$		
$\Phi$	<i>true</i>	



```

void f(int x) {

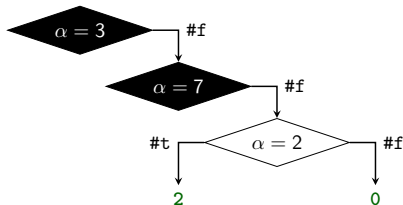
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;

    }
    *
    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	2	$\alpha$
$arr$	{3, 7, 2}	
$i$	2	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha = 2)$	





```

void f(int x) {

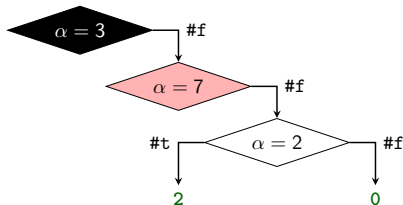
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;

    }
    *
    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	2	$\alpha$
$arr$	{3, 7, 2}	
$i$	2	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha \neq 7) \wedge (\alpha = 2)$	

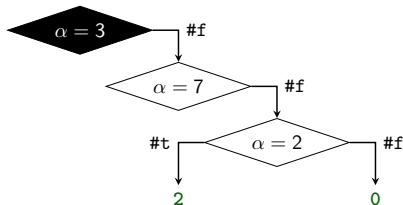


$(\alpha \neq 3) \wedge (\alpha = 7)$  is **SAT**  
when  $x = 7$

# Example – Loops

```
void f(int x) {  
    *  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
        if (arr[i] == x) break;  
        i++;  
    }  
  
    return i;  
}
```

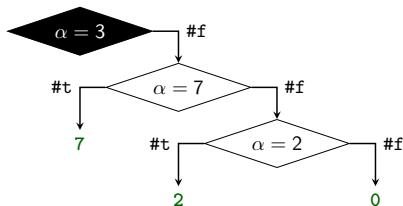
$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	7	$\alpha$
$arr$		
$i$		
$\Phi$	true	



# Example – Loops

```
void f(int x) {  
  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
  
        if (arr[i] == x) break;  
        i++;  
  
    }  
    *  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	7	$\alpha$
$arr$	{3, 7, 2}	
$i$	1	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha = 7)$	



```

void f(int x) {

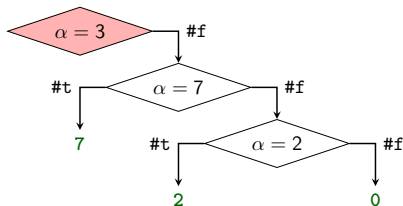
    int arr[] = {3, 7, 2};
    int i = 0;

    while (i < 3) {

        if (arr[i] == x) break;
        i++;

    }
    *
    return i;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	7	$\alpha$
$arr$	{3, 7, 2}	
$i$	1	
$\Phi$	$(\alpha \neq 3) \wedge (\alpha = 7)$	

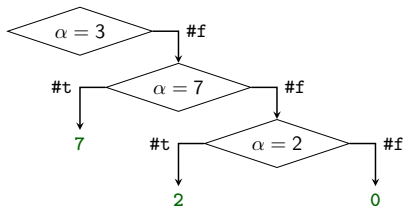


$(\alpha = 3)$  is **SAT**  
when  $x = 3$

# Example – Loops

```
void f(int x) {  
    *  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
        if (arr[i] == x) break;  
        i++;  
    }  
  
    return i;  
}
```

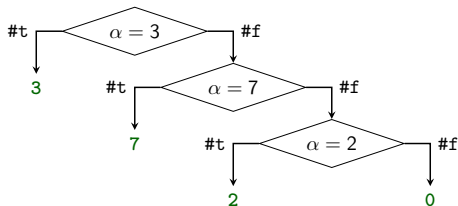
$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	3	$\alpha$
$arr$		
$i$		
$\Phi$	<i>true</i>	



# Example – Loops

```
void f(int x) {  
  
    int arr[] = {3, 7, 2};  
    int i = 0;  
  
    while (i < 3) {  
  
        if (arr[i] == x) break;  
        i++;  
  
    }  
    *  
    return i;  
}
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	3	$\alpha$
$arr$	{3, 7, 2}	
$i$	0	
$\Phi$	$(\alpha = 3)$	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {
    *
    if (x > 0)

        if (p != NULL)

            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$p$	NULL	$\beta$
$\Phi$	true	

```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

        if (p != NULL)

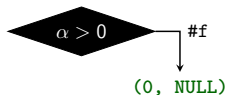
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    *
    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$p$	NULL	$\beta$
$\Phi$	$(\alpha \leq 0)$	





```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

        if (p != NULL)

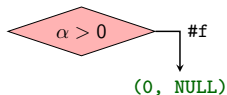
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

                *
            return 0;
    }
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	0	$\alpha$
$p$	NULL	$\beta$
$\Phi$	$(\alpha \leq 0)$	



$(\alpha > 0)$  is **SAT**  
 when  $(x, p) = (42, \text{NULL})$

```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {
    *
    if (x > 0)

        if (p != NULL)

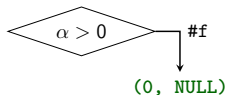
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	NULL	$\beta$
$\Phi$	true	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)
        *
        if (p != NULL)

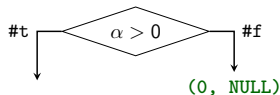
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	NULL	$\beta$
$\Phi$	$(\alpha > 0)$	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

        if (p != NULL)

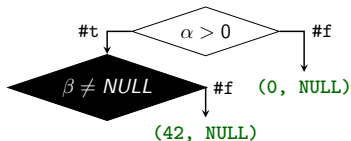
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

                *
            return 0;
    }
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	NULL	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta = \text{NULL})$	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

        if (p != NULL)

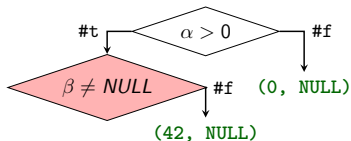
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

                *
            return 0;
    }
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	NULL	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta = \text{NULL})$	



$(\alpha > 0) \wedge (\beta \neq \text{NULL})$  is **SAT**  
 when  $(x, p) = (42, 0xA0BF : \boxed{0} \mid \boxed{\text{NULL}})$

```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {
    *
    if (x > 0)

        if (p != NULL)

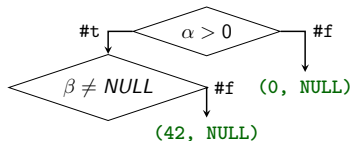
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	0xA0BF : 0   NULL	$\beta$
$\Phi$	true	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

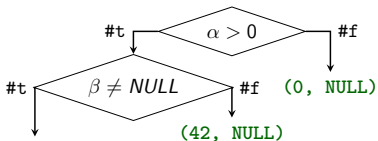
        if (p != NULL)
            *
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

        return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	42		$\alpha$
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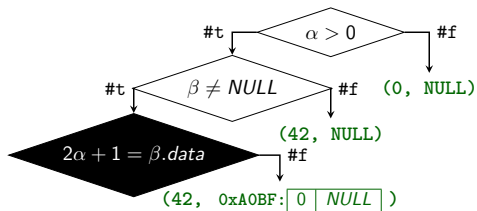
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    *
    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
$p$	0xA0BF : 0   NULL	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta \neq \text{NULL}) \wedge (2\alpha + 1 \neq \beta.\text{data})$	





```

class Node {
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};

void f(int x, Node *p) {

    if (x > 0)

        if (p != NULL)

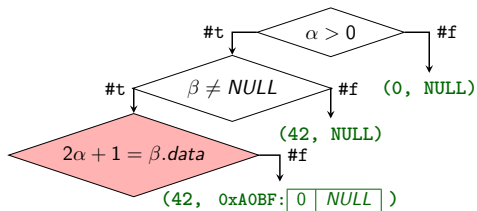
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$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	42	$\alpha$
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$\Phi$	$(\alpha > 0) \wedge (\beta \neq \text{NULL}) \wedge$ $(2\alpha + 1 \neq \beta.\text{data})$	



$(\alpha > 0) \wedge (\beta \neq \text{NULL})$   
 $\wedge (2\alpha + 1 = \beta.\text{data})$  is **SAT**

when  $(x, p) = (1, 0xA0BF : [ 3 | \text{NULL} ])$

```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {
    *
    if (x > 0)

        if (p != NULL)

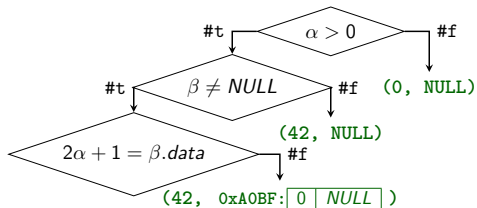
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$	$\Omega$
$x$	1	$\alpha$
$p$	0xA0BF : 3   NULL	$\beta$
$\Phi$	true	



```

class Node {
    int data;
    Node* next;
};

void f(int x, Node *p) {

    if (x > 0)

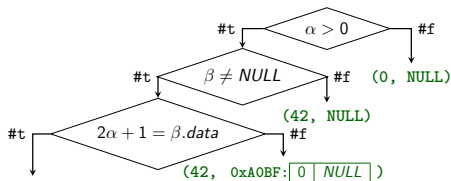
        if (p != NULL)

            if (x*2+1 == p->data)
                *
                if (p->next == p)

                    ERROR;

            return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	1		$\alpha$
$p$	0xA0BF :	3   NULL	$\beta$
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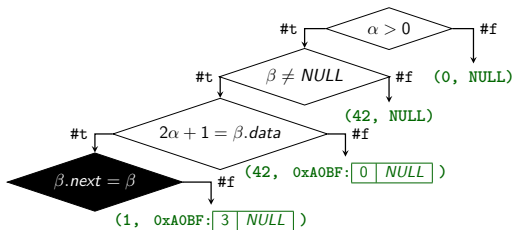
            if (x*2+1 == p->data)

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                    ERROR;

    *
    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	1		$\alpha$
$p$	0xA0BF :	3   NULL	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta \neq \text{NULL}) \wedge$ $(2\alpha + 1 = \beta.\text{data}) \wedge (\beta.\text{next} \neq \beta)$		



```

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void f(int x, Node *p) {

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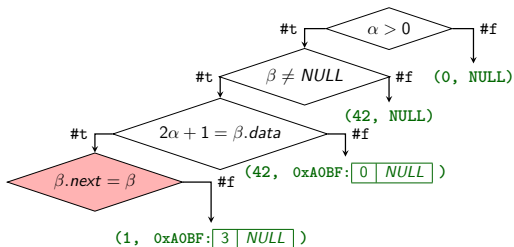
            if (x*2+1 == p->data)

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                    ERROR;

    *
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}
    
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$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	1		$\alpha$
$p$	0xA0BF :	3   NULL	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta \neq \text{NULL}) \wedge$ $(2\alpha + 1 = \beta.\text{data}) \wedge (\beta.\text{next} \neq \beta)$		



$(\alpha > 0) \wedge (\beta \neq \text{NULL})$   
 $\wedge (2\alpha + 1 = \beta.\text{data})$  is **SAT**

when  $(x, p) = (1, 0xA0BF : \boxed{3} \mid \boxed{0xA0BF})$

```

class Node {
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void f(int x, Node *p) {
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    if (x > 0)

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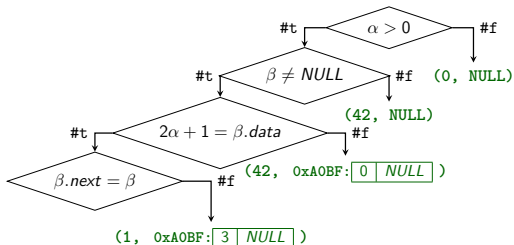
            if (x*2+1 == p->data)

                if (p->next == p)

                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	1		$\alpha$
$p$	0xA0BF :	3   0xA0BF	$\beta$
$\Phi$	true		



```

class Node {
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};

void f(int x, Node *p) {

    if (x > 0)

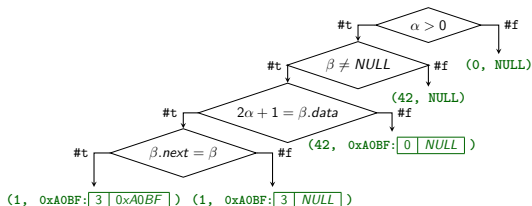
        if (p != NULL)

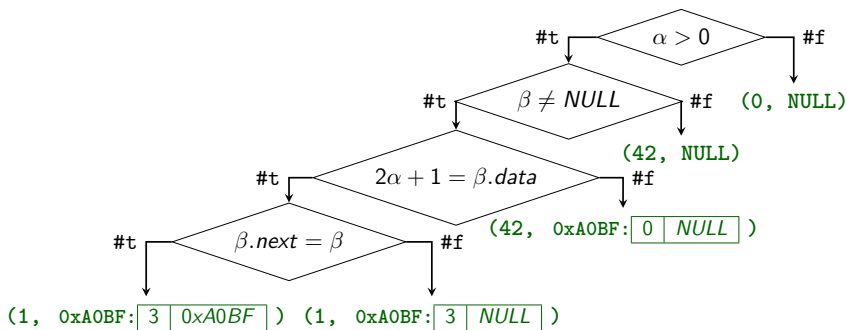
            if (x*2+1 == p->data)

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                    ERROR;

    return 0;
}
    
```

$\mathbb{X}$	$\mathbb{V}$		$\Omega$
$x$	1		$\alpha$
$p$	0xA0BF : 3	0xA0BF	$\beta$
$\Phi$	$(\alpha > 0) \wedge (\beta \neq \text{NULL}) \wedge$ $(2\alpha + 1 = \beta.\text{data}) \wedge (\beta.\text{next} = \beta)$		







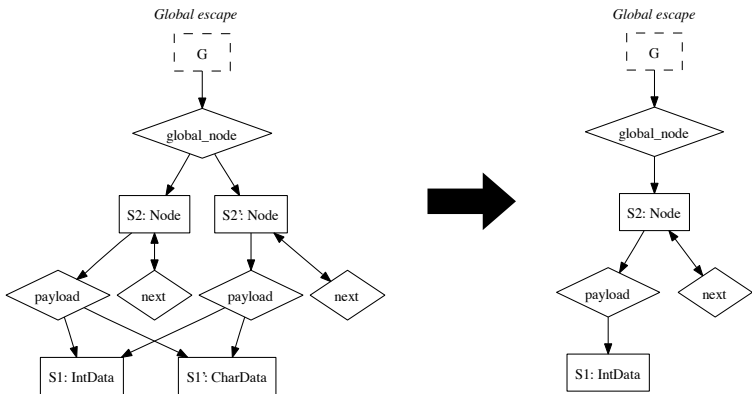
- [KLEE](#) – LLVM based DSE engine.
- [Jalangi2](#) – JavaScript dynamic analysis framework by Samsung.
- [S2E](#) – Platform for symbolic execution of binary code (x86, ARM).
- [CutEr](#) – Concolic unit testing tool for Erlang.

- Many efforts have combined dynamic and static analysis, yielding **blended** or **hybrid** analysis techniques.

- Many efforts have combined dynamic and static analysis, yielding **blended** or **hybrid** analysis techniques.
- Some hybrid analyses use information recorded during dynamic executions of the program to improve the static-analysis precision. However, they are **generally unsound** because they rely on incomplete information.
- Some recent hybrid analyses have been proposed a **combined interpretation** to address the unsoundness issue, and it interchanges between **concrete** and **abstract interpretations** to improve the precision.

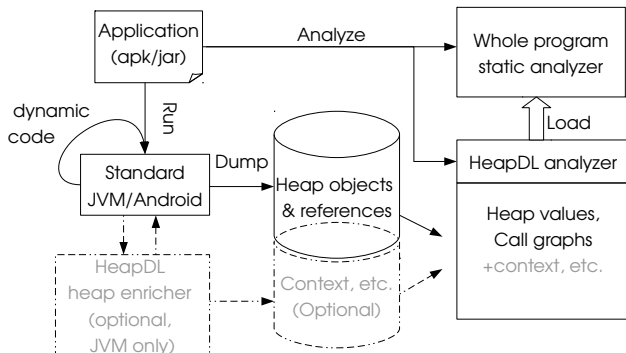
[ISSTA'07] Dufour et al., “Blended analysis for performance understanding of framework-based applications”

- **Escape Analysis** – A static analysis technique that determines whether an object can escape the scope of the method or a thread.



[OOPSLA'17] Grech et al., “Heaps Don’t Lie: Countering Unsoundness with Heap Snapshots”

- **Heap Snapshots** – A technique that records the whole-heap snapshots during program execution and then uses them to guide the static analysis. (especially for Android and JVM applications)

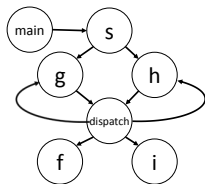


[PLDI'16] Briana M. Ren and Jeffrey S. Foster, "Just-in-time Static Type Checking for Dynamic Languages"

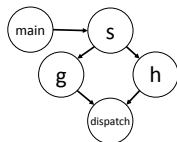
- **Just-in-time Static Type Checking** – A technique that type checks Ruby code even in the presence of meta-programming.
- It **dynamically gathers method type signatures** and utilizes them in **static type checking** of their body when they are invoked.

```
class Talk < ActiveRecord::Base
  belongs_to :owner, :class_name => "User"
  ....
  type :owner?, "(User) → %bool"
  def owner?(user)
    return owner == user
  end
end
```

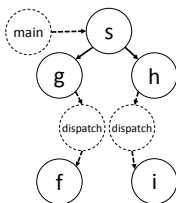
[POPL'18] J. Toman and D. Grossman, "Concerto: a framework for combined concrete and abstract interpretation"



(a) Sound but Imprecise Call-Graph



(b) Unsound Call-Graph

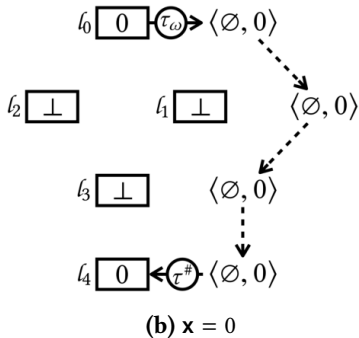


(c) Call-Graph with Concerto

[ESEC/FSE'21] J. Park et al., "Accelerating JavaScript Static Analysis via Dynamic Shortcuts"

- **Dynamic Shortcuts** – A technique to perform **sealed execution** (dynamic analysis) during the static analysis to accelerate and increase the precision of the analysis without losing soundness.

- $\ell_0$  if (  $x \geq 0$  )
- $\ell_1$   $x = x$ ;
- else
- $\ell_2$   $x = -x$ ;
- $\ell_3$   $x = -x$ ;
- $\ell_4$

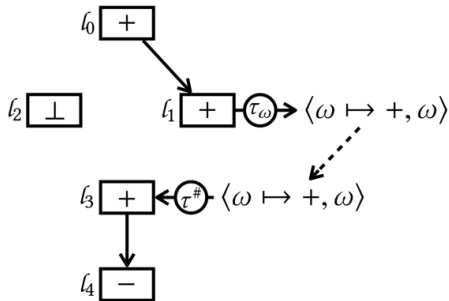




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- $\ell_3$   $x = -x$ ;
- $\ell_4$

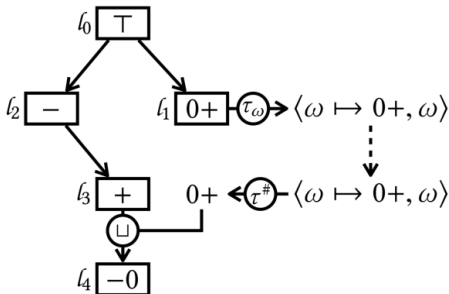


(c)  $x > 0$

[ESEC/FSE'21] J. Park et al., "Accelerating JavaScript Static Analysis via Dynamic Shortcuts"

- **Dynamic Shortcuts** – A technique to perform **sealed execution** (dynamic analysis) during the static analysis to accelerate and increase the precision of the analysis without losing soundness.

- $l_0$  if (  $x \geq 0$  )
- $l_1$   $x = x$ ;
- else
- $l_2$   $x = -x$ ;
- $l_3$   $x = -x$ ;
- $l_4$



(d)  $x \in \mathbb{N}$

## 1. Symbolic Execution

- Basic Idea

- Satisfiability Modulo Theories (SMT)

- Limitations of Symbolic Execution

## 2. Dynamic Symbolic Execution (DSE)

- Search Heuristics

- Example – Hash Function

- Example – Loops

- Example – Data Structures

- Realistic Implementation

- Other Hybrid Analysis Techniques

- Lecture for Dynamic Symbolic Execution by Prof. Mayur Naik at UPenn CIS.

<https://software-analysis-class.org/lectures/lecture14>

- [CSUR'18] Baldoni et al., “A Survey of Symbolic Execution Techniques”

<https://dl.acm.org/doi/abs/10.1145/3182657>

- Mutation Testing

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<https://plrg.korea.ac.kr>