

# Lecture 4 – Identifiers (1)

## COSE212: Programming Languages

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2024 Fall

- **ADT** for **Abstract Syntax** of AE

```
enum Expr:  
  case Num(number: BigInt)  
  case Add(left: Expr, right: Expr)  
  case Mul(left: Expr, right: Expr)
```

- **Parser** for **Concrete Syntax** of AE

```
lazy val expr: P[Expr] = ...
```

- **Interpreter** for **Semantics** of AE

```
def interp(expr: Expr): Value = ...
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- **Parser** for **Concrete Syntax** of AE

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lazy val expr: P[Expr] = ...
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- **Interpreter** for **Semantics** of AE

```
def interp(expr: Expr): Value = ...
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- In this lecture, we will learn **identifiers**.

## 1. Identifiers

- Bound Identifiers

- Free Identifiers

- Shadowing

## 2. VAE – AE with Variables

- Concrete Syntax

- Abstract Syntax

- Examples

## 1. Identifiers

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An **identifier** is a **name** for a certain element in a program.

In Scala, there are diverse kinds of identifiers:

```
/* Scala */  
  
// variable names  
val x: Int = 42  
  
// function and parameter names  
def f(a: Int, b: Int): Int = a + b  
  
// class and field names  
case class Person(name: String, age: Int)  
  
...
```

```
/* Scala */  
val x: Int = 3  
  
val y: Int = x + z  
  
def add(a: Int, b: Int): Int =  
  val x: Int = a + b  
  x + add(y, z)  
  
add(x, b)
```

A **bound identifier** is an identifier that is **defined** in a program.

- A **binding occurrence** of an identifier denotes its **definition** site.
- A **scope** of an identifier denotes where the identifier is **usable**.
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```
/* Scala */  
val x: Int = 3  
  
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  x + add(y, z)  
  
add(x, b)
```

Binding  
Occurrences

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val x: Int = 3  
  
val y: Int = x + z  
  
def add(a: Int, b: Int): Int =  
  val x: Int = a + b  
  x + add(y, z)  
  
add(x, b)
```

The diagram illustrates the scope of the identifier `x`. A red dashed line points from the `x` in the first `val` declaration to the `x` in the `add` function definition. A red box encloses the `add` function definition and the `add(x, b)` call, with the word "scope" written in red above it.

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/* Scala */  
val x: Int = 3  
  
val y: Int = x + z  
  
scope  
def add(a: Int, b: Int): Int =  
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Let's draw arrows from each bound occurrence to its binding occurrence.

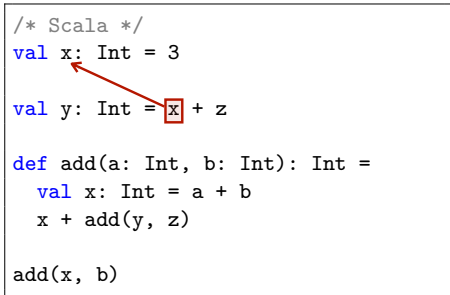


```
/* Scala */
val x: Int = 3

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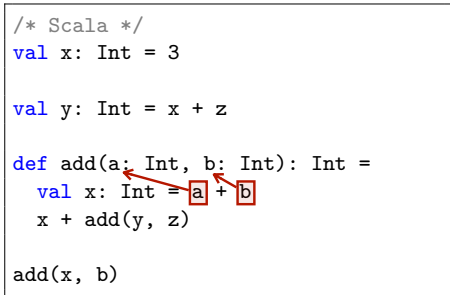
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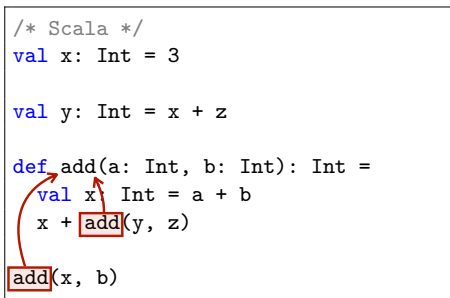
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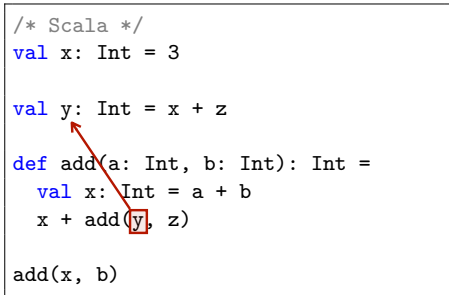
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val x: Int = 3

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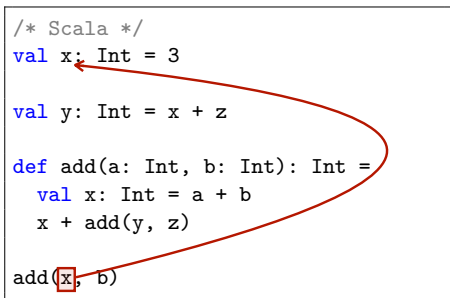


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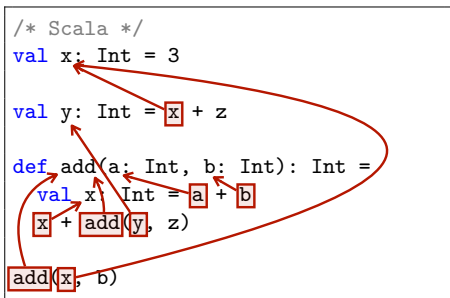
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val x: Int = 3  
  
val y: Int = x + z  
  
def add(a: Int, b: Int): Int =  
  val x: Int = a + b  
  x + add(y, z)  
  
add(x, b)
```

Free  
Identifiers

A **free identifier** is an identifier that is **not defined** in the current scope of the program.



```
/* Scala */
val x: Int = 3
val y: Int = x + z
def add(a: Int, b: Int): Int =
  val x: Int = a + b
  x + add(y, z)
add(x, b)
```

Annotations in the code:

- Shadowed Identifier**: points to the `x` in `val x: Int = 3`
- Shadowing**: points to the `x` in `val x: Int = a + b`
- Shadowing Identifier**: points to the `x` in `add(x, b)`

**Shadowing** means that the innermost binding occurrence shadows the outer binding occurrences of the same name.

- A **shadowing identifier** is an identifier that shadows another
- A **shadowed identifier** is an identifier that is shadowed by another.

```
/* Scala */
val x: Int = 3
val y: Int = x + z
def add(a: Int, b: Int): Int =
  val x: Int = a + b
  x + add(y, z)
add(x, b)
```

Annotations in the image:

- Shadowed Identifier**: points to the first `x` in `val x: Int = 3`.
- Shadowing**: points to the second `x` in `val x: Int = a + b`.
- Shadowing Identifier**: points to the `x` in `add(x, b)`.

**Shadowing** means that the innermost binding occurrence shadows the outer binding occurrences of the same name.

- A **shadowing identifier** is an identifier that shadows another
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Note that shadowing is **NOT** a mutation.

## 1. Identifiers

Bound Identifiers

Free Identifiers

Shadowing

## 2. VAE – AE with Variables

Concrete Syntax

Abstract Syntax

Examples

Now, we want to extend AE into VAE with **variables**:

```
/* VAE */  
val x = 1 + 2; // x = 1 + 2 = 3  
val y = x + 3; // y = x + 3 = 3 + 3 = 6  
y + 4          // 6 + 4 = 10
```

Now, we want to extend AE into VAE with **variables**:

```
/* VAE */  
val x = 1 + 2; // x = 1 + 2 = 3  
val y = x + 3; // y = x + 3 = 3 + 3 = 6  
y + 4          // 6 + 4 = 10
```

First, we define the **concrete syntax** of **identifiers** used in VAE:

```
<digit>      ::= "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9"  
<number>    ::= "-"? <digit>+  
<alphabet>  ::= "A" | "B" | "C" | ... | "Z" | "a" | "b" | "c" | ... | "z"  
<idstart>   ::= <alphabet> | "_"  
<idcont>    ::= <alphabet> | "_" | <digit>  
<keyword>   ::= "val"  
<id>        ::= <idstart> <idcont>* butnot <keyword>
```

Now, we want to extend AE into VAE with **variables**:

```
/* VAE */
val x = 1 + 2; // x = 1 + 2 = 3
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<number>    ::= "-"? <digit>+
<alphabet>  ::= "A" | "B" | "C" | ... | "Z" | "a" | "b" | "c" | ... | "z"
<idstart>   ::= <alphabet> | "_"
<idcont>    ::= <alphabet> | "_" | <digit>
<keyword>   ::= "val"
<id>        ::= <idstart> <idcont>* butnot <keyword>
```

For example, the following are valid identifiers:

x      y      get\_name      getName      add42

Then, let's define the **concrete syntax** of VAE in BNF:

```
<expr> ::= <number>
         | <expr> "+" <expr>
         | <expr> "*" <expr>
         | "(" <expr> ")"
         | "{" <expr> "}"
         | "val" <id> "=" <expr> ";" <expr>
         | <id>
```

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```

Note that each variable definition creates a **new scope**.



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         | "val" <id> "=" <expr> ";" <expr>
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```

Note that each variable definition creates a **new scope**. For example:

```
/* VAE */
val x = 1 + 2;
val y = x + 3;
y + 4
```

Then, let's define the **concrete syntax** of VAE in BNF:

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<expr> ::= <number>
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         | "{" <expr> "}"
         | "val" <id> "=" <expr> ";" <expr>
         | <id>
```

Note that each variable definition creates a **new scope**. For example:

```
/* VAE */
val x = 1 + 2;
val y = x + 3;
y + 4
```

means

```
/* VAE */
val x = 1 + 2;
{ // scope of x
  val y = x + 3;
  { // scope of y
    y + 4
  }
}
```

Let's define the **abstract syntax** of VAE in BNF:

Numbers	$n \in \mathbb{Z}$	(BigInt)	Expressions	$e ::= n$	(Num)
Identifiers	$x \in \mathbb{X}$	(String)		$e + e$	(Add)
				$e * e$	(Mul)
				<code>val <math>x = e</math>; <math>e</math></code>	(Val)
				$x$	(Id)

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Numbers	$n \in \mathbb{Z}$	(BigInt)	Expressions	$e ::= n$	(Num)
Identifiers	$x \in \mathbb{X}$	(String)		$e + e$	(Add)
				$e * e$	(Mul)
				$\text{val } x = e; e$	(Val)
				$x$	(Id)

We can define an **ADT** for the abstract syntax of VAE in Scala:

```
enum Expr:  
  case Num(number: BigInt)  
  case Add(left: Expr, right: Expr)  
  case Mul(left: Expr, right: Expr)  
  // variable definition  
  case Val(name: String, init: Expr, body: Expr)  
  // variable lookup  
  case Id(name: String)
```

```
enum Expr:  
  case Num(number: BigInt)  
  case Add(left: Expr, right: Expr)  
  case Mul(left: Expr, right: Expr)  
  case Val(name: String, init: Expr, body: Expr)  
  case Id(name: String)
```

Parser implementation is given and you don't need to implement it.

You can freely use Expr to parse VAE programs as follows:

```
Expr("val x = 1; x + 2")  
// Val("x", Num(1), Add(Id("x"), Num(2)))  
  
Expr("val a = 1; val b = 2; a + b")  
// Val("a", Num(1), Val("b", Num(2), Add(Id("a"), Id("b"))))
```

For each VAE program, please draw:

- an **arrow** from each **bound occurrence** to its **binding occurrence**.
- a **dotted arrow** from each **shadowing variable** to its **shadowed one**.
- an **X** mark on each **free variable**.

```
/* VAE */  
val x = 1; x
```

```
/* VAE */  
val x = x + 1;  
val y = x * 2;  
val x = y + x;  
x * z
```

```
/* VAE */  
val x = 1;  
val y = {  
    val x = 2 * x;  
    { val y = x; y } + { val y = 3; y }  
};  
x + y
```

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- Abstract Syntax

- Examples

- Identifiers (2)

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